

# CS4400/5400

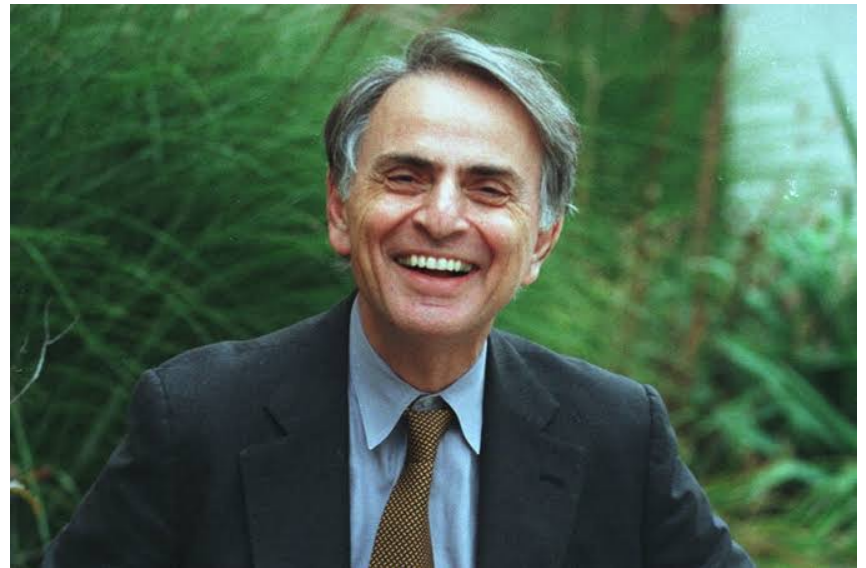
# Programming $\lambda$ anguages

Spring 2024

Instructor: Steven Holtzen

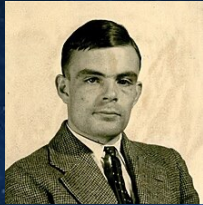
[s.holtzen@northeastern.edu](mailto:s.holtzen@northeastern.edu)

“If you wish to make an apple pie from scratch, you must first invent the universe.”



Carl Sagan

November 9, 1934 -- December 20, 1996



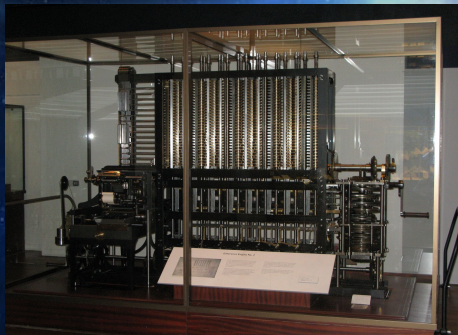
Alan Turing  
1912 – 1954  
Turing Machine (1936)



Alonzo Church  
1903 – 1995  
Lambda Calculus (1930s)



Ada Lovelace  
1815 – 1842  
First Programmer



Babbage Difference Engine

# Tiny Computers, Tiny Languages





The ENIAC Computer  
1945

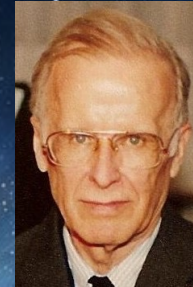
First **programmable** digital  
computer

First program:  
feasibility of nuclear weapons

## AUTODOCDE

1952, Alick Glennie

First **compiled** programming language



FORTRAN

John Backus

1953



LISP

John McCarthy

1960



## ALGOL

1958

Designed by committee



FLOW-MATIC/COBOL

Grace Hopper

1954

# 1950s: The Dawn of the Digital Era



# Smalltalk

Object-oriented programming  
Mid 1970s

# C++

1980

# Prolog

Logic programming  
1972

# C

1972



# SQL

1978

# ML

Statically typed functional language  
1973

# Growth of Digital Computers



**Python**

1990

**Haskell**

1990

**Java**

1995

**Go**

2009

Smalltalk

C++



Prolog



C



ML

**Julia**

2012

**JavaScript**

1995

SQL

**TypeScript**

2012

**Rust**

2015

**Swift**

2014

**The Modern Era**

# Questions

Why are there so many programming languages?

Which language should I learn? Should I use?

Are some languages worse than others? Better?  
How can I compare them?

What distinguishes one language from another?

Why are new languages being made today?

How are new languages made?

# Why study programming languages?

- Be a *more effective programmer*
  - How to *choose languages* for your problems
  - How to *design and implement languages* when needed
- Become equipped to *learn new languages quickly*
- Be *prepared for an evolving world*
  - New languages are showing up all the time
- Enjoy an *aesthetic journey* through this elegant field (subjective)



# What is a “programming language”?

“A programming language is a system of notation for writing computer programs.”



[https://en.wikipedia.org/wiki/Programming\\_language](https://en.wikipedia.org/wiki/Programming_language)

Accessed Friday, January 5

# What is a “programming language”?

“Computer programming language, any of various languages for expressing a set of detailed instructions for a digital computer.”



<https://www.britannica.com/technology/computer-programming-language>

Accessed Friday, January 5

A programming language has two parts:

## Syntax

What does a program look like?



Ancient Mesopotamia

## Semantics

What does a program do?

“Your debt  
is canceled”



A programming language has two parts:

## Syntax

What does a program look like?

Python

```
x = 5  
print(x)
```

## Semantics

What does a program do?

- Create a variable called “x”
- Print the contents of that variable

A programming language has two parts:

## Syntax

What does a program look like?

JavaScript

```
let x = 5;  
console.log(x)
```

## Semantics

What does a program do?

- Create a variable called “x”
- Print the contents of that variable

A programming language has two parts:

## Syntax

What does a program look like?

OCaml

```
let x = 5 in  
Format.printf "%s" x
```

## Semantics

What does a program do?

- Create a variable called “x”
- Print the contents of that variable



# This course is all about *precisely defining programming languages*

## Syntax

What does a program look like?

Formal descriptions as  
grammars

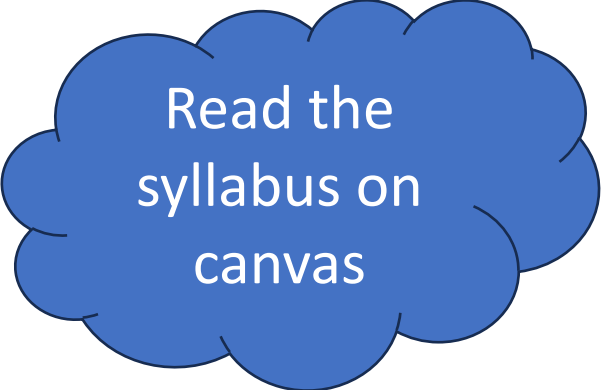
## Semantics

What does a program do?

Programs that run  
programs

**Interpreters!**

- Grow big languages out of small ones
- Implement new languages



Read the  
syllabus on  
canvas

# Course Logistics & Content

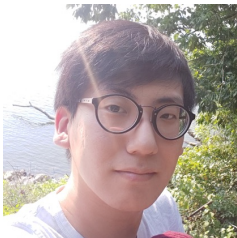
- Course resources, staff, and policies
- Course modules and overview
- Grading and evaluation

# Course Staff

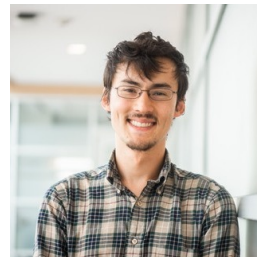
- Instructor: Steven Holtzen
  - Assistant Professor at Northeastern since 2021
  - This is my first time teaching this course



- Teaching Assistants



Minsung Cho  
PhD. Student  
[minsung@ccs.neu.edu](mailto:minsung@ccs.neu.edu)



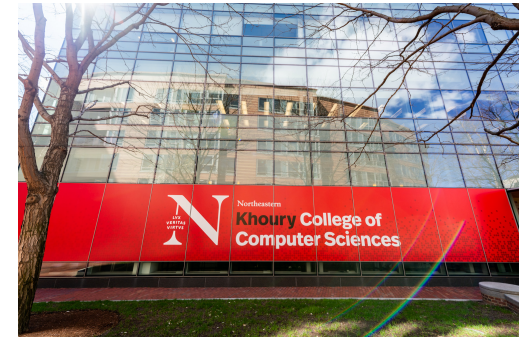
Sam Stites  
PhD. Student  
[stites.s@northeastern.edu](mailto:stites.s@northeastern.edu)



Jack Czenszak  
PhD. Student  
[czenszak.j@northeastern.edu](mailto:czenszak.j@northeastern.edu)

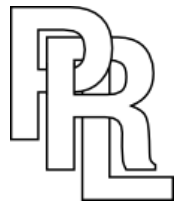


You are at one of the  
best schools for PL  
in the world



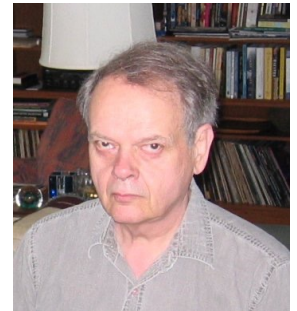
<https://prl.khoury.northeastern.edu/people.html>

Many of the tools we use in this  
class were developed here!



# Module 0: Plait

“Most programming languages — including the most widely used — have serious design defects, so that learning such languages is less a matter of mastering a style than of learning workarounds for the language designer’s mistakes... I believe that the most reasonable approach to this problem is to first learn to program in a single well-designed programming language (or perhaps a small number of stylistically varied well-designed languages) that imposes a minimal number of obstacles to the programming task”



**John C. Reynolds**  
**1935 -- 2017**

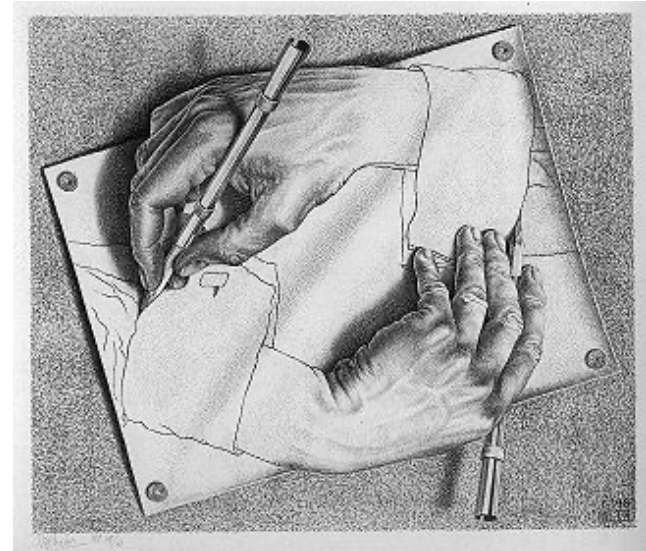
*Some Thoughts on Teaching Programming  
and Programming Languages, 2012*

# Module 0: Plait Learning Objectives

1. Become familiar with *functional programming* and how to solve problems in a *functional style*
2. Become familiar with a *typed language* and *programming with types*
3. Gain practice *learning a new language from scratch*

# Module 1: Growing an interpreter

- We will grow the *syntax* and *semantics* of a tiny core language called SMO<sub>L</sub> (Standard Model of Languages)
  - We will *program interpreters* for this language in Plait
- Language features include:
  - Conditionals, scope and binding, first-class functions, macros, object, state



*Drawing Hands*  
M. C. Escher 1968

# Module 2: Types

- Types are form of ***checked specification*** for programs
- Example: Java

```
import java.util.Scanner;

public class HelloWorld {

    public static void main(String[] args) {

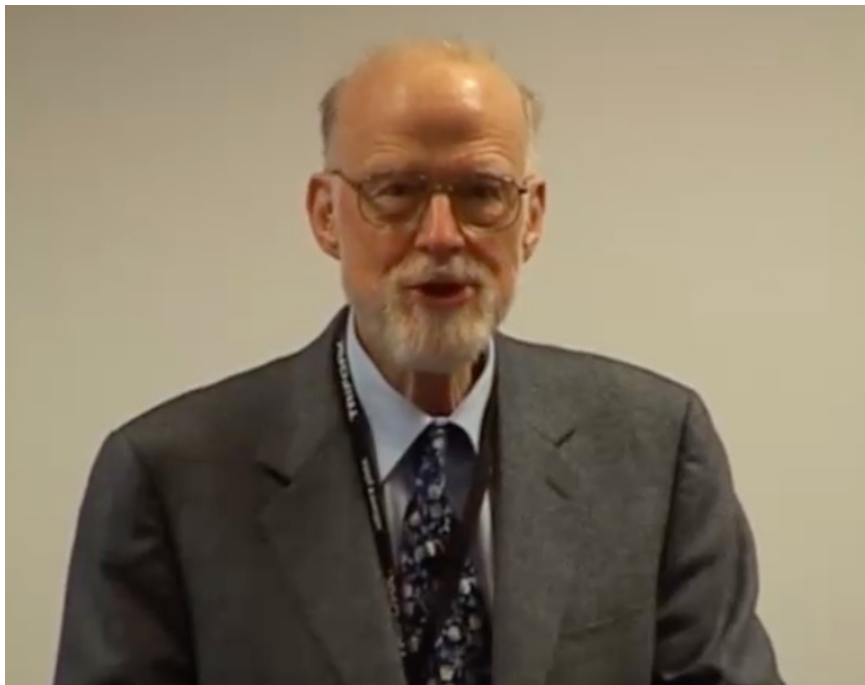
        // Creates a reader instance which takes
        // input from standard input – keyboard
        Scanner reader = new Scanner(System.in);
        System.out.print("Enter a number: ");

        // nextInt() reads the next integer from the keyboard
        int number = reader.nextInt();

        // println() prints the following line to the output
        System.out.println("You entered: " + number);

    }
}
```





Tony Hoare

Types can't prevent all bugs:  
this is a valid Java program:

```
public class Example {  
  
    public static void main(String[] args) {  
        Object obj = null;  
        obj.hashCode();  
    }  
  
}
```

# Null References: The Billion Dollar Mistake

Tony Hoare

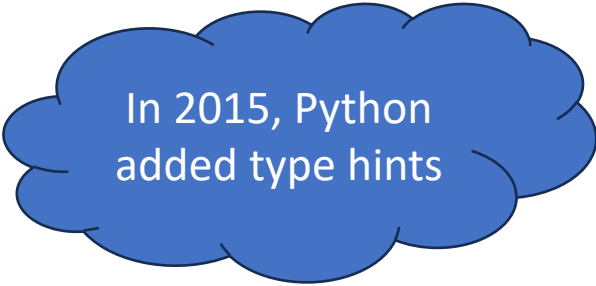
Recommended viewing:

<https://www.infoq.com/presentations/Null-References-The-Billion-Dollar-Mistake-Tony-Hoare/>

# Module 2: Why study types?

- You ***will*** encounter types in your day-to-day programming

```
def greeting(name: str) -> str:  
    return 'Hello ' + name
```



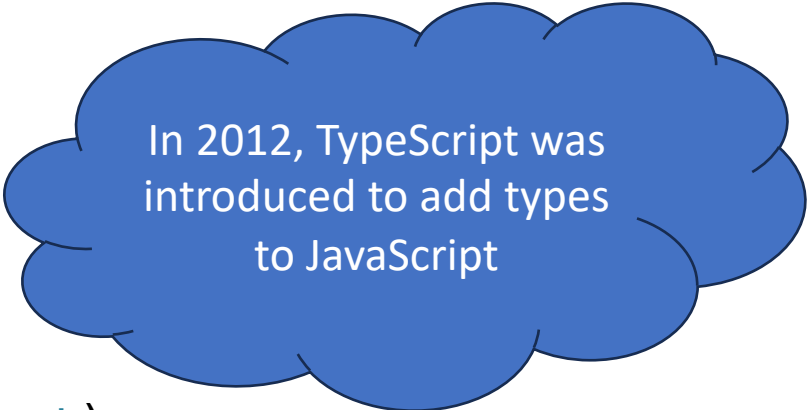
In 2015, Python  
added type hints

# Module 2: Why study types?

- You **will** encounter types in your day-to-day programming

```
interface Account {  
  id: number  
  displayName: string  
  version: 1  
}
```

```
function welcome(user: Account)  
{  
  console.log(user.id)  
}
```



In 2012, TypeScript was introduced to add types to JavaScript

# Module 2: Types

- We will build our own type system for SMOl
  - Learn the formal properties of type systems
- Study ***type inference*** and techniques to make programming with types easier
- Encounter the rich ***mathematical structure*** of types
  - What formal properties can a type system give you?

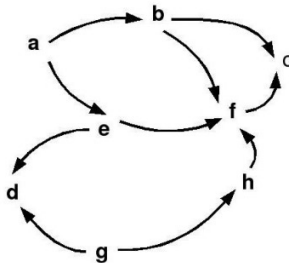


\* Subject to change

# Module 3: Beyond SMOl\*

- We will study advanced languages and language features that go beyond SMOl
  - Implement and program some interesting languages

```
a(g,h).  
a(g,d).  
a(e,d).  
a(h,f).  
a(e,f).  
a(a,e).  
a(a,b).  
a(b,f).  
a(b,c).  
a(f,c).
```



Laziness

Logic programming

Goal: Broaden your horizons on what programming languages can look like



# Schedule overview

- Available here:

<https://docs.google.com/spreadsheets/d/e/2PACX-1vQNTDbNs-WnG7YU5iebht9XuWfTNF2LBSPWzU1ctif8YrNuciQWZDtZU2hviaFt22asf1C2O27tdOoe/pubhtml?gid=0&single=true>

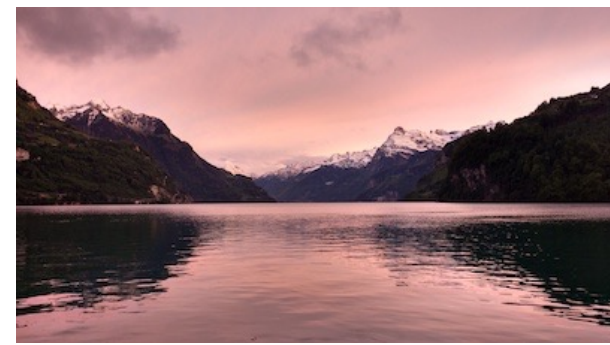
CS4400 Spring'24 Schedule : Sheet1

Module	Date	Lecture title	Topics	Resources
Introduction to Plait and Functional Programming	Monday Jan 8	Introduction and course overview	- Why programming languages? - A first look at Racket/Plait	<a href="https://docs.racket-lang.org/plait/Tutorial.html">https://docs.racket-lang.org/plait/Tutorial.html</a> Sections 1.1 -- 1.5
	Wednesday Jan 10	Programming in Racket and Plait	- Solving problems functionally and recursively - How to write tests in Plait - How Plait's type system works	<a href="https://docs.racket-lang.org/plait/Tutorial.html">https://docs.racket-lang.org/plait/Tutorial.html</a> Sections 1.1 -- 1.8
	Monday Jan 15	<b>No Class --- Martin Luther King Jr. Day</b>		
	Wednesday Jan 17	<b>No Class --- Steven Traveling for POPL</b>	- Optional in-class workshop on Plait	
Building a SMoL Interpreter	Monday Jan 22	Abstract Syntax	- Abstract syntax trees - A simple calculator language - Interpreting a language by hand	PLAI pg. 17 -- 27 See <a href="https://www.plai.org/3/2/PLAI%20Version%203.2.2%20printing.pdf">https://www.plai.org/3/2/PLAI%20Version%203.2.2%20printing.pdf</a>
	Wednesday Jan 24	Evaluation	- Implementing and testing the evaluator - Parsing and s-expressions	PLAI pg. 28 -- 37
	Monday Jan 29	Conditionals	- Extending the syntax with `if` - Design space of `if` - Adding Booleans, the `Value` type	PLAI pg. 37 -- 47
	Wednesday Jan 31	Local binding	- The `let` syntax - Scope - An evaluator for `let`	PLAI pg. 47 -- 57
	Monday Feb 5	First-class functions	- Syntax for functions - Adding functions to the `Value` type - Evaluating functions	PLAI pg. 58 -- 69
	Wednesday Feb 7	Growing SMoL: Macros	- Desugaring - An example: Strict If - define-syntax - Macro stepping in DrRacket	PLAI pg. 71 -- 84
Monday Feb 12	Objects I	- The "standard model" of objects - State - Access control	PLAI pg. 85 -- 95	

# Schedule overview

Types	Wednesday Feb 14	Objects II	- Extending objects: mixins, traits	PLAI pg. 97 -- 106
	Monday Feb 19	Introduction to types	- What are types? - A simple type checker - How to read and write typing judgments	PLAI pg. 109 -- 122
	Wednesday Feb 21	Typing functions	- The typing rule for functions - Assume-guarantee reasoning - Making a typechecker - Handling recursion	PLAI pg. 123 -- 132
	Monday Feb 26	The Simply Typed Lambda Calculus	- Syntax and a type checker - The Omega term and normalization	
	Wednesday Feb 28	Safety and soundness	- What is type safety, why do you want it - Enforcing type safety - Type safety for simply-typed lambda calculus	PLAI pg. 133 -- 144
	Monday Mar 4	<b>No Class -- Spring Break</b>		
	Wednesday Mar 6	<b>No Class -- Spring Break</b>		
	Monday Mar 11	Type inference	- Basic goals of type inference - Hindley-Milner - Complexity of type inference	PLAI pg. 145 -- 149
	Wednesday Mar 13	Algebraic datatypes and pairs	- Typechecking algebraic datatypes and pairs - Proofs and programs: Curry-Howard	PLAI pg. 150 -- 153
	Monday Mar 18	Subtyping	- Adding subtyping to typing judgments - Applications: information flow analysis	PLAI pg. 165 -- 170
	Wednesday Mar 20	Gradual typing	- TypeScript, typed Python, Typed Racket	PLAI pg. 170 -- 176
Paradigms	Monday Mar 25	Logic Programming I	- Programming with relations - Unification - A simple type checker	PLAI pg. 178 -- 184
	Wednesday Mar 27	Logic Programming II		PLAI pg. 193 -- 202
	Monday Apr 1	Laziness I	- Evaluation schemes: eager, lazy, call-by-need, call by name - Consequences of evaluation schemes - A lazy evaluator - Programming in lazy languages	
	Wednesday Apr 3	Laziness II	- Modeling state and mutation - A taste of Haskell	
	Monday Apr 8	Effects I	- Effects in Racket - Effect handlers	
	Wednesday Apr 10	Effects II		
	Monday Apr 15	<b>No Class -- Patriot's day</b>		
	Wednesday Apr 17	Slack day		

# Textbook



- *Programming Languages: Application and Interpretation*, Third Edition, by Shriram Krishnamurthy
- Open-access textbook, available at:  
<https://www.plai.org/>
- We will follow it closely: you are encouraged to read the textbook sections ahead or after lecture as a reference

# Prerequisites

- Required: CS3500 (Object oriented design) or Equivalent
- Highly recommended:
  - Experience programming in at least one major programming language
  - This will be a programming-intensive course

# Input/Output

- Important course announcements will be broadcast as Canvas Announcements
  - You should check to make sure that you receive these
- We will use Piazza
  - Please ask all course questions there
  - You can ask private questions
  - You should have received an email invitation
- Notes/slides will be posted on Canvas after lecture



# Assignments and grading

Type	Frequency	Percent of Final Grade
Homework	About once a week	60%
Quizzes	About 4	40%

Range	> 93	[90,93)	[87, 90)	[83, 87)	[80, 83)	[77, 80)	[73, 77)	[70, 73)	[67, 70)	[60, 67)	<50
Grade	A	A-	B+	B	B-	C+	C	C-	D+	D	F

Note: Some assignments / problems will be marked as “CS5400”. These are only for students enrolled in CS5400.

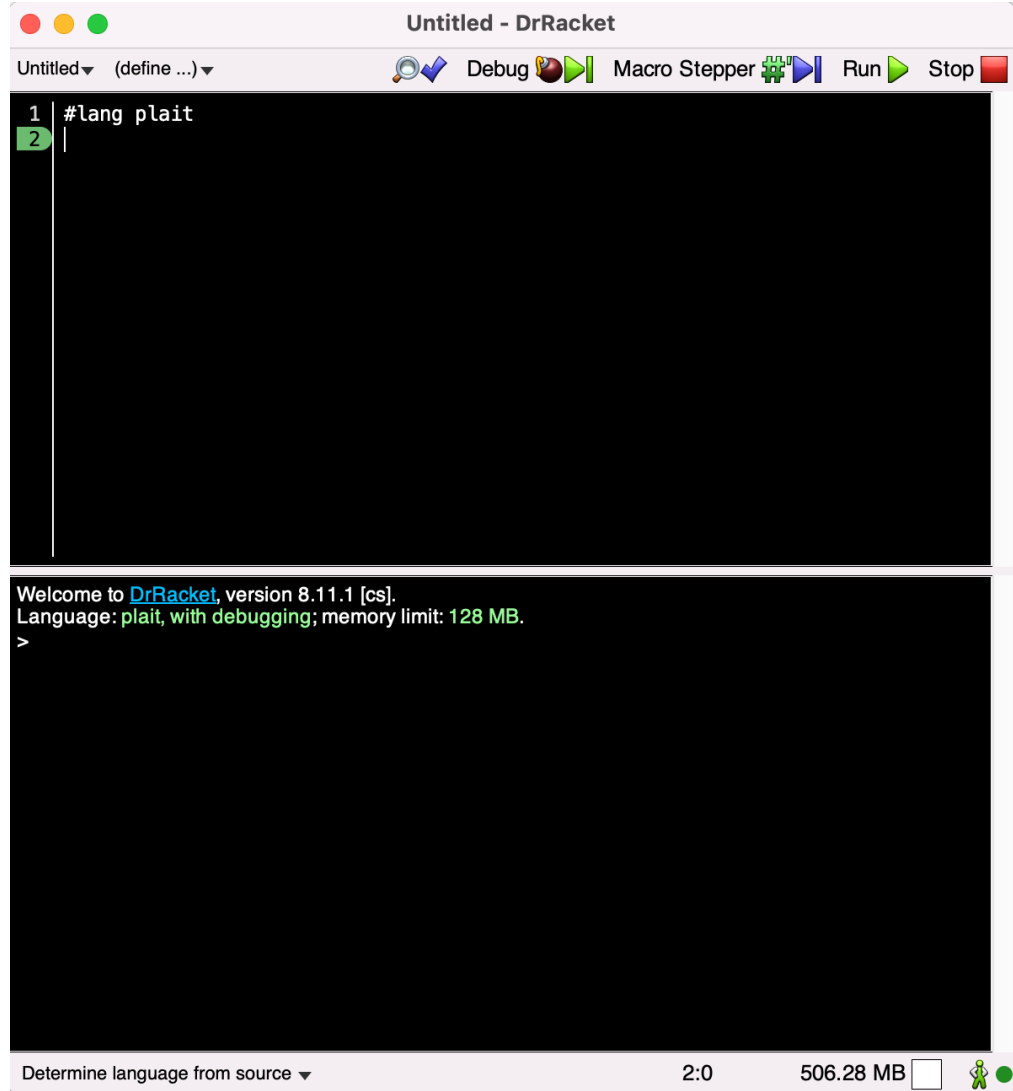
# A taste of Plait

Goals:

- Set up and install Plait
- Understand how to write small Plait programs and call functions
- Know the key properties of Plait

# Setting up Plait

- Follow <https://docs.racket-lang.org/plait/getting-started.html>
- Download DrRacket (use version 8.11.1)
- You will need to install the Plait .plt file



The screenshot shows the DrRacket IDE interface. The title bar reads "Untitled - DrRacket". The menu bar includes "Untitled", "(define ...)", "Debug", "Macro Stepper", "Run", and "Stop". The editor area contains the following code:

```
1 #lang plait
2 |
```

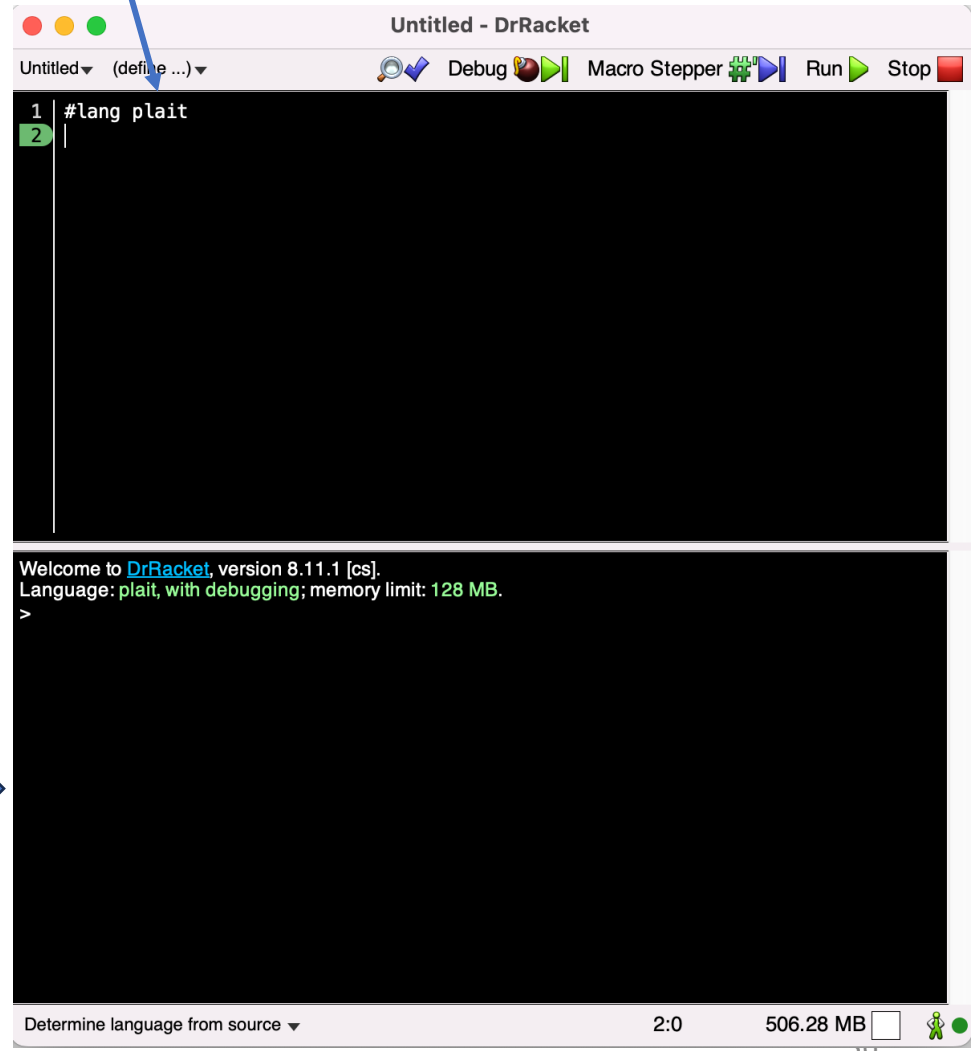
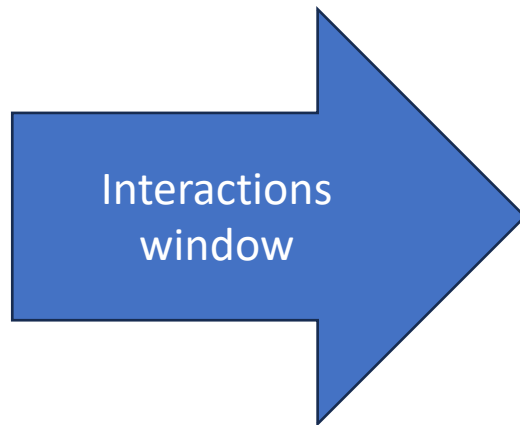
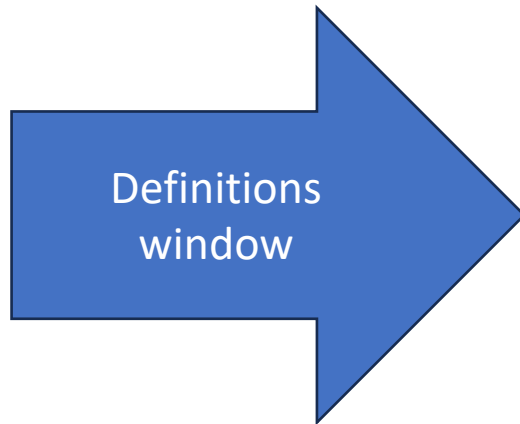
The output area below the editor displays the following text:

```
Welcome to DrRacket, version 8.11.1 [cs].
Language: plait, with debugging; memory limit: 128 MB.
>
```

The status bar at the bottom shows "Determine language from source", "2:0", "506.28 MB", and a small icon of a person.


# DrRacket

Tells DrRacket which programming language to use



# Plait Resources

- Plait website: <https://docs.racket-lang.org/plait/>
- Plait tutorial: <https://docs.racket-lang.org/plait/Tutorial.html>
- YouTube video tutorial: <https://www.youtube.com/playlist?list=PLbdXd8eufjyUT8rza1qDcS0RUnRTr9A1f>
- Plait CheatSheet on Canvas
- Ask on Piazza if you get stuck :)



Plait is a tiny language made specifically for this course! We can learn it in a few hours...



# Simple data

- Enter code into the Interaction window and press “enter” to run your code
- Basic data types:
  - Numbers 1, 1.2, 1/3
  - Strings “quoted”
  - Symbols 'a, 'b, 'sym, ...
  - Booleans #t #f
- Comments begin with ;

```
> 4
- Number
4
> "hello"
- String
"hello"
> 'a
- Symbol
'a
> #t
- Boolean
#t
> #f
- Boolean
#f
```

Input Plait program called a **term** or **expression**

**Type** of entered term; every term has a type

**Value** program evaluates to

An unusual type; we will see more of it later

# Calling functions

- Adding two numbers:
  - Unusual syntax! We will come to appreciate it.

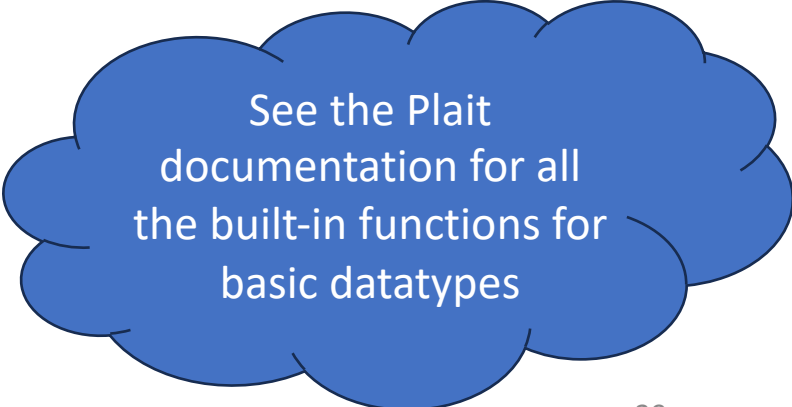
```
> (+ 1 2)
- Number
3
```

- Some built-in functions for integers:

```
> (max 1 2)
- Number
2
```

```
> (- 2 3)
- Number
-1
```

```
> (< 10 20)
- Boolean
#t
```



See the Plait documentation for all the built-in functions for basic datatypes

# Calling functions

- Chaining together functions:

```
> (+ 1 (max 3 4))  
- Number  
5
```

- A note on floating point:

```
> (eq? (/ 1.0 3.0) 1/3)  
- Boolean  
#f
```

- Be careful! Plait represents these two values differently

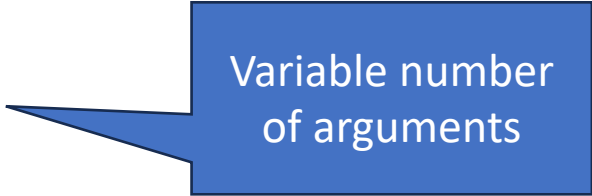
```
> 1/3  
- Number  
1/3
```

```
> (/ 1.0 3.0)  
- Number  
0.3333333333333333
```

# Some functions on Booleans

```
> (and #t #f)  
- Boolean  
#f
```

```
> (and #t #t #f)  
- Boolean  
#f
```



Variable number  
of arguments

```
> (or #f #t)  
- Boolean  
#t
```

```
> (not #t)  
- Boolean  
#f
```

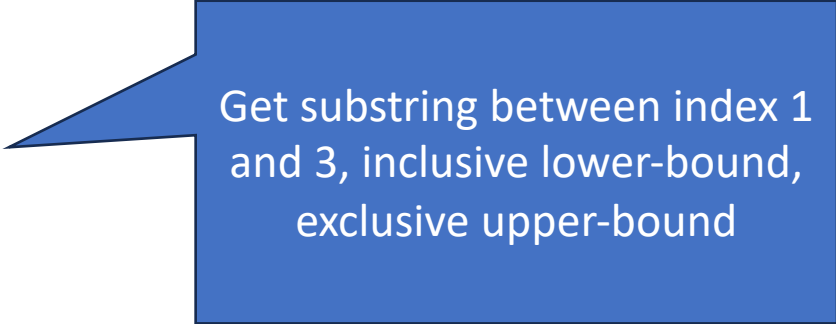
```
> (eq? #t #f)  
- Boolean  
#f
```

# Some functions on Strings

```
> (equal? "hello" "world")  
- Boolean  
#f
```

```
> (string-append "hello"  
"world")  
- String  
"helloworld"
```

```
> (substring "hello" 1 3)  
- String  
"el"  
>
```



Get substring between index 1 and 3, inclusive lower-bound, exclusive upper-bound

# Types

- Plait functions expect their arguments to have certain types

**Type signature** says the max function takes two Number as input and returns a Number

```
> max
- (Number Number -> Number)
#<procedure:max>
```

- If you call a function with the wrong type of arguments, Plait will help you by complaining

```
> (max 1 "oops")
✖ typecheck failed: Number vs. String in:
max
"oops"
```

# if expressions

(if guard thn els)  
If the guard is true,  
evaluate thn; otherwise,  
evaluate els

```
> (if #t "woohoo" "ohno")  
- String  
"woohoo"
```

```
> (if #t "what" 10)  
typecheck failed: String vs. Number in:  
  "what"  
  10
```

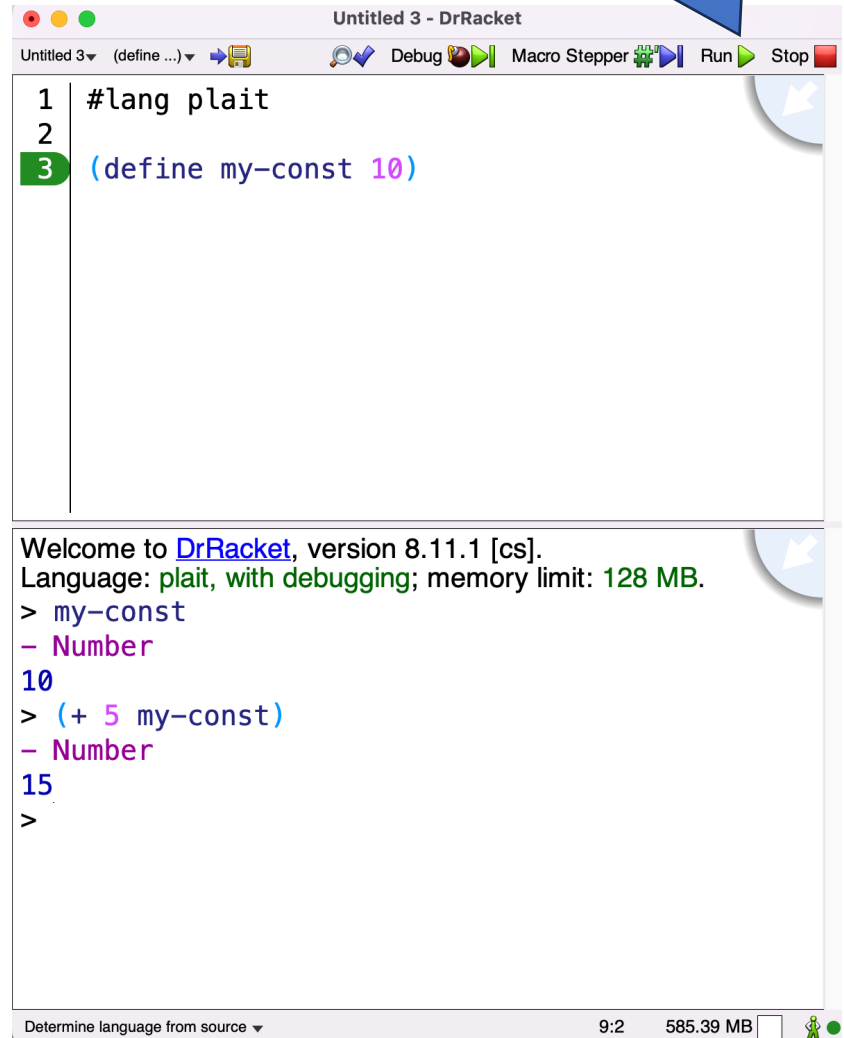
if requires that both thn  
and els terms be the  
same type

```
> (if (< 10 20) 'ok 'oops)  
- Symbol  
'ok
```

# Definitions

Press “run” to run the definitions pane

- Syntax:  
(define id e)
- `id` is an identifier, `e` is a Plait expression
- Creates a globally accessible constant called `id`



The screenshot shows the DrRacket IDE interface. The top window, titled "Untitled 3 - DrRacket", contains a code editor with the following Racket code:

```
1 #lang plait
2
3 (define my-const 10)
```

The bottom window shows the interaction window with the following output:

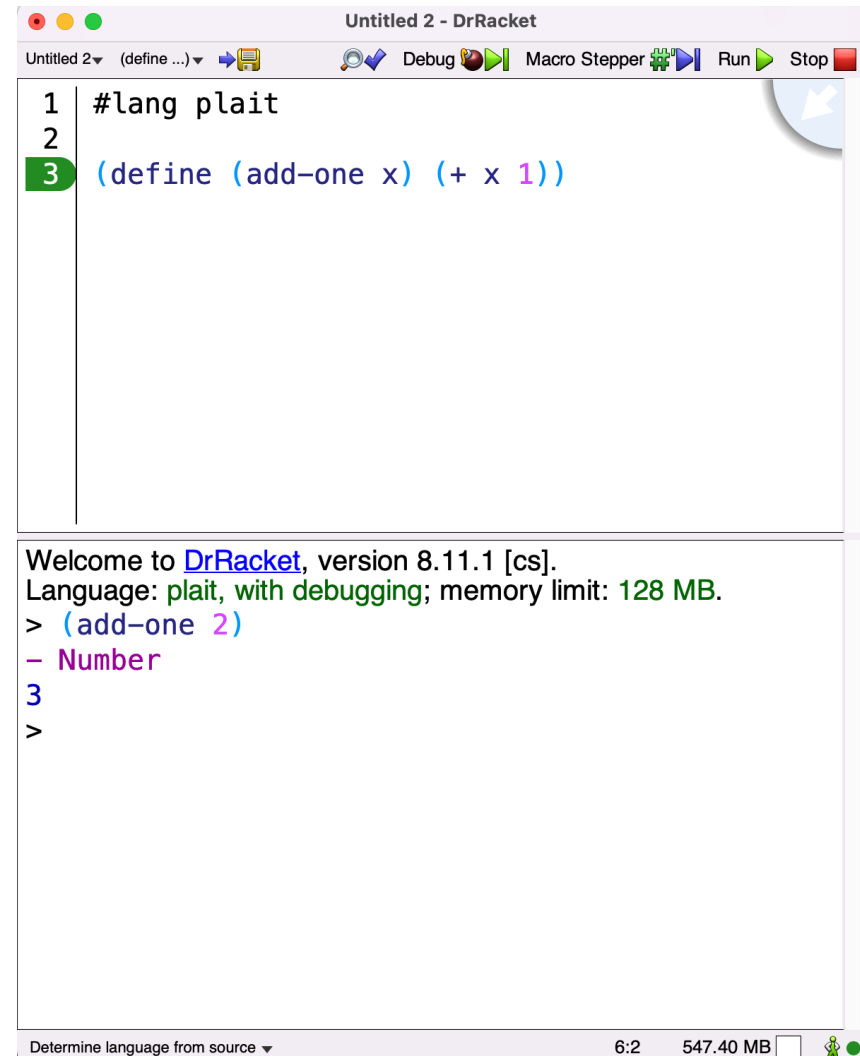
```
Welcome to DrRacket, version 8.11.1 [cs].
Language: plait, with debugging; memory limit: 128 MB.
> my-const
- Number
10
> (+ 5 my-const)
- Number
15
>
```

The status bar at the bottom indicates "Determine language from source", "9:2", and "585.39 MB".



# Defining functions

- **Syntax:**  
`(define (id arg1 arg2 ...) e)`
- Creates a globally accessible function called `id` with arguments `arg1`, `arg2`, ... and body `e`



The screenshot shows the DrRacket IDE interface. The top window, titled "Untitled 2 - DrRacket", contains the following code:

```
1 #lang plait
2
3 (define (add-one x) (+ x 1))
```

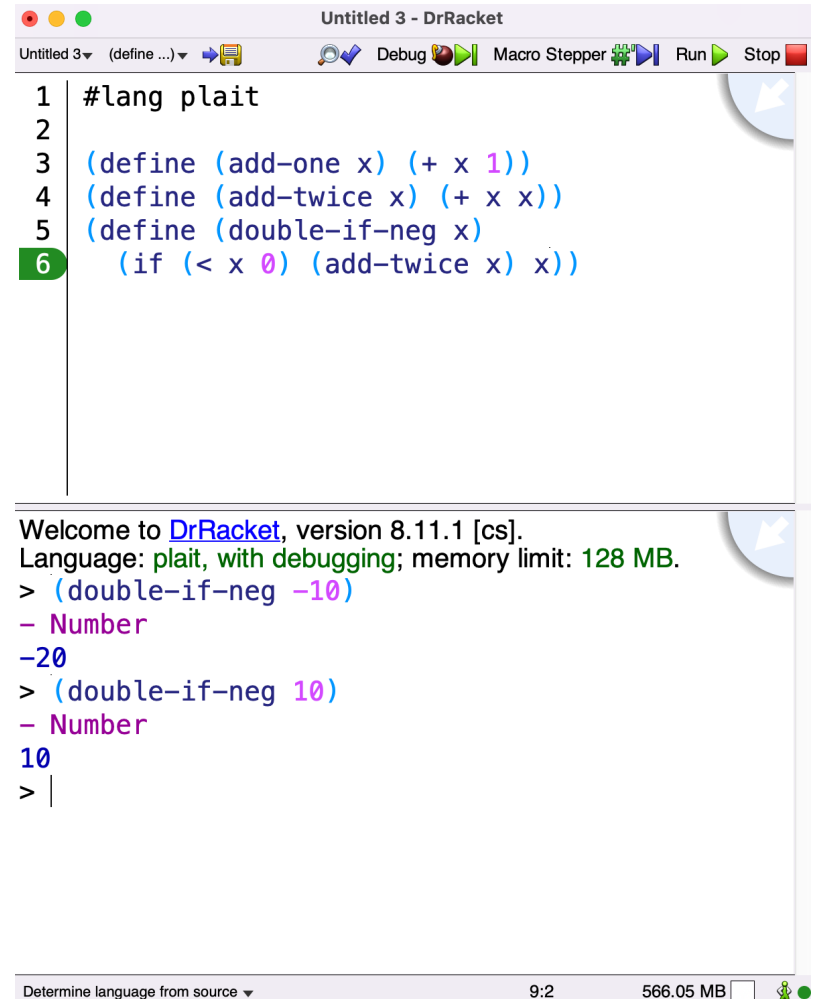
The bottom window shows the execution output:

```
Welcome to DrRacket, version 8.11.1 [cs].
Language: plait, with debugging; memory limit: 128 MB.
> (add-one 2)
- Number
3
>
```

The status bar at the bottom indicates "Determine language from source", "6:2", and "547.40 MB".

# Defining functions

- Write a function “double-if-neg” that takes a number as an argument, and returns double that number if it is negative, otherwise return the input number



```
Untitled 3 - DrRacket
Untitled 3 (define ...)
Debug Macro Stepper Run Stop

1 #lang plait
2
3 (define (add-one x) (+ x 1))
4 (define (add-twice x) (+ x x))
5 (define (double-if-neg x)
6   (if (< x 0) (add-twice x) x))

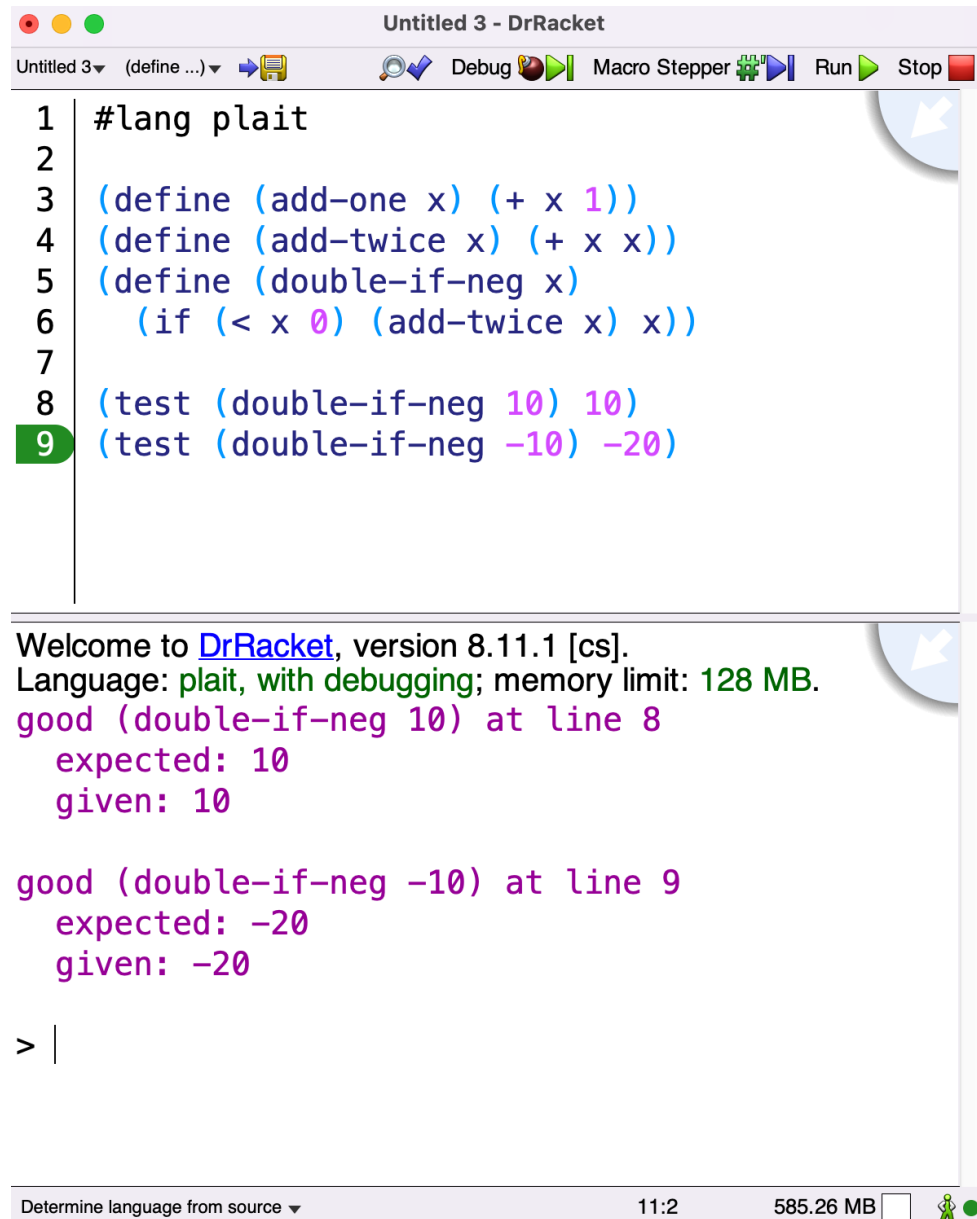
Welcome to DrRacket, version 8.11.1 [cs].
Language: plait, with debugging; memory limit: 128 MB.
> (double-if-neg -10)
- Number
-20
> (double-if-neg 10)
- Number
10
> |

Determine language from source 9:2 566.05 MB
```

# Testing

(test e1 e2)

tests that e1 and e2  
evaluate to the same  
value



```
Untitled 3 - DrRacket
Untitled 3 (define ...) Debug Macro Stepper Run Stop
1 #lang plait
2
3 (define (add-one x) (+ x 1))
4 (define (add-twice x) (+ x x))
5 (define (double-if-neg x)
6   (if (< x 0) (add-twice x) x))
7
8 (test (double-if-neg 10) 10)
9 (test (double-if-neg -10) -20)

Welcome to DrRacket, version 8.11.1 [cs].
Language: plait, with debugging; memory limit: 128 MB.
good (double-if-neg 10) at line 8
  expected: 10
  given: 10

good (double-if-neg -10) at line 9
  expected: -20
  given: -20

> |

Determine language from source 11:2 585.26 MB
```

# Conclusion

- Homework is due this Friday (Jan 12)
- Before next lecture:
  - Download DrRacket and install Plait
  - Try the first 2 homework problems
- Next time:
  - Bring a computer that is setup with Plait ready to do some in-class activities
  - We will see more Plait and practice solving more interesting problems