

CS4400/5400
Programming λ anguages

Lecture 4

Parsing and conditionals

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Goals for today

1. Finish parsing and running `calc` programs
 - Host semantics
 - How to read grammars
 - Parsing s-expressions
2. Develop `cond`, extending `calc` with conditionals
 - See the design space of if-expressions
 - Create an evaluator for `cond`
 - The `value` datatype

Logistics

- New homework released tonight
 - Due next Wednesday (Jan 31), recommend you start
- Reminder: course materials on course webpage now instead of Canvas (see link on canvas)
 - All slides, code, etc. goes there
- I've been tweaking the schedule a bit based on our pace, check it for latest reading
- Reminder: I am fairly closely following PLAI, use it as a resource

Syntax and semantics of `calc`

Abstract syntax

```
(define-type Exp
  [num (n : Number)]
  [plus (left : Exp)
        (right : Exp)])
```

Semantics

```
(calc : (Exp -> Number))
(define (calc e)
  (type-case Exp e
    [(num n) n]
    [(plus e1 e2)
     (+ (calc e1)
        (calc e2))]))
```

Host semantics

- I never actually told you what syntactic “+” did

```
(calc : (Exp -> Number))
(define (calc e)
  (type-case Exp e
    [(num n) n]
    [(plus e1 e2)
     (+ (calc e1)
        (calc e2))]))
```

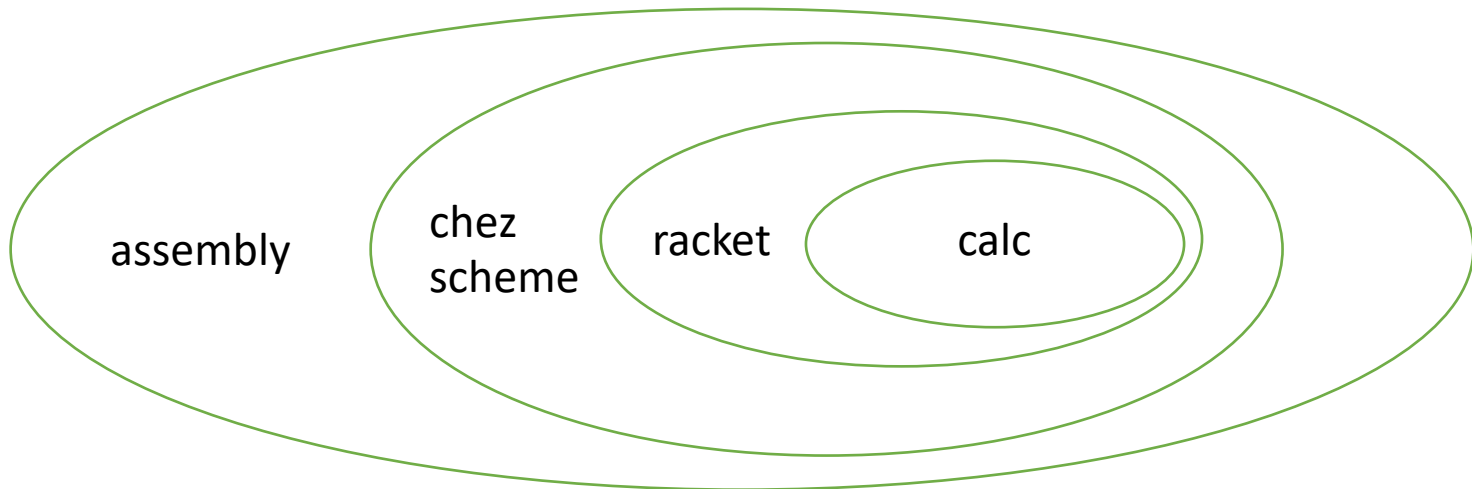
- The semantics of “plus” in `calc` is inherited from Plait’s semantics of “+”
- `calc` *inherited the host semantics* of “+” from Plait

Host semantics

- Q: What is Plait's semantics of “+”?
- A: A function of type
(Number Number \rightarrow Number)
- Takes two arguments of Plait type Number and produces their arithmetic sum
 - There are alternative semantics of “+”: perhaps it permits concatenating strings, etc...

Host semantics

- In turn, Plait's semantics of "+" are inherited from Racket...
 - ... which is inherited from Chez scheme...
 - ... which is inherited from the assembly language instruction standard for running addition...

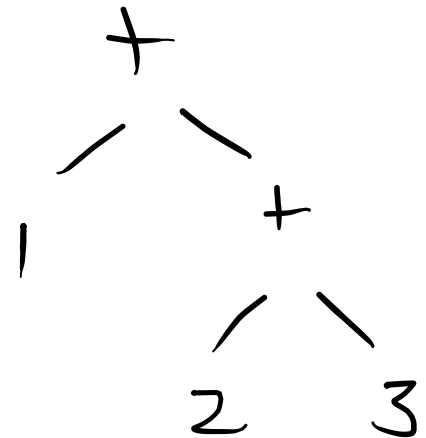


Parsing & grammars

- Goal of parsing: given a **surface syntax** description of a program, generate an **abstract syntax tree**

(+ 1 (+ 2 3))

Parsing



How do we describe surface syntax? We call a description of surface syntax a **grammar**

Describing grammars in English

- An `calc` expression is either:
 - A number
 - A string of the form “(“ followed by “+” followed by an expression followed by an expression followed by “)”
- This gets quite unwieldy to write down as our language gets increasingly complex
- The designers of ALGOL60 agreed, so designed a system for describing surface syntax grammars called **Backus-Naur Form**

Describing Surface Syntax with Backus-Naur Form (BNF)

- BNF is a lightweight notation for describing surface syntax

```
<plus> ::= (+ <e> <e>)  
<e>    ::= num | <plus>  
<start> ::= <e>
```

- This grammar captures our English description of calc expressions
 - The symbol <e> is called a **non-terminal**
 - The symbol num is called a terminal: it is defined to be any syntactic Plait number (0.1, 10, 1/2, ...)
 - One symbol is designated as the start symbol

BNF and Plait Datatypes

- There is a one-to-one map between a BNF and our abstract syntax tree datatype in Plait
 - The BNF includes details about the text (i.e., contains characters)

```
<plus> ::= (+ <e> <e>)  
<e>    ::= num | <plus>  
<start> ::= <e>
```

```
(define-type Exp  
  [num (n : Number)]  
  [plus (left : Exp) (right : Exp)]  
)
```

Parsing with BNF

```
<plus> ::= (+ <e> <e>)  
<e>    ::= num | <plus>  
<start> ::= <e>
```

<e>

(+ 1 (+ 2 3))

Parsing with BNF

```
<plus> ::= (+ <e> <e>)  
<e>    ::= num | <plus>  
<start> ::= <e>
```

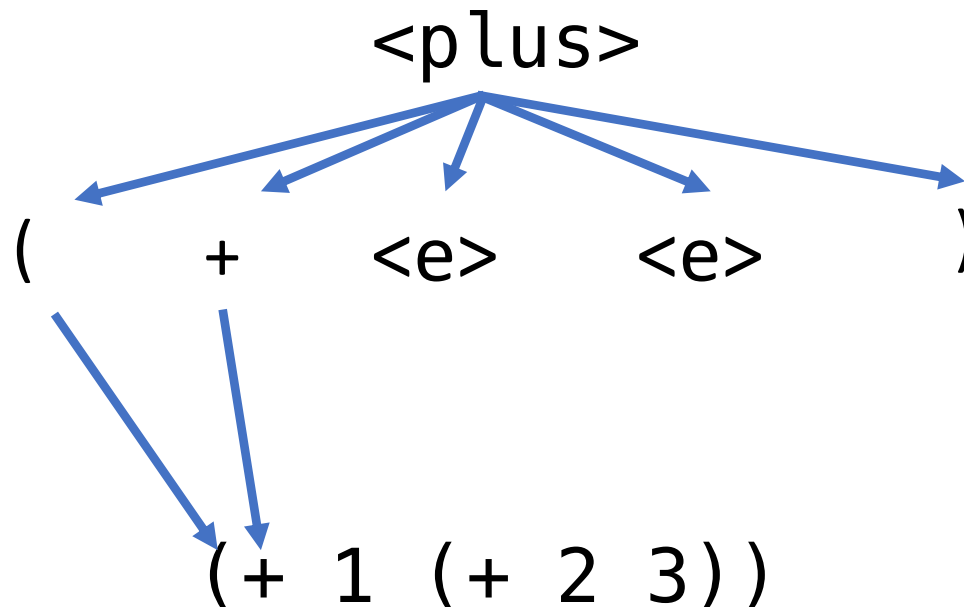
num? no



(+ 1 (+ 2 3))

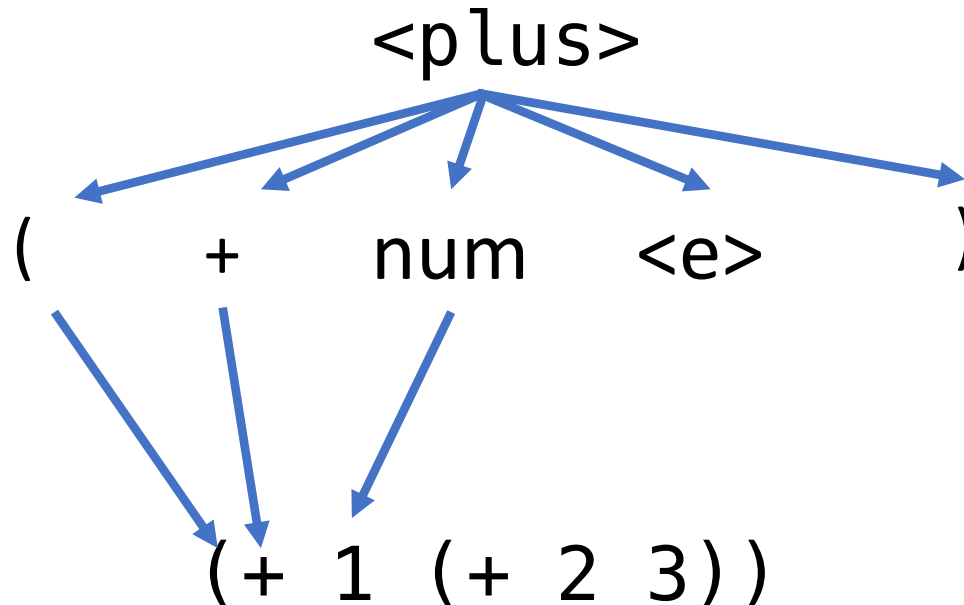
Parsing with BNF

`<plus> ::= (+ <e> <e>)`
`<e> ::= num | <plus>`
`<start> ::= <e>`



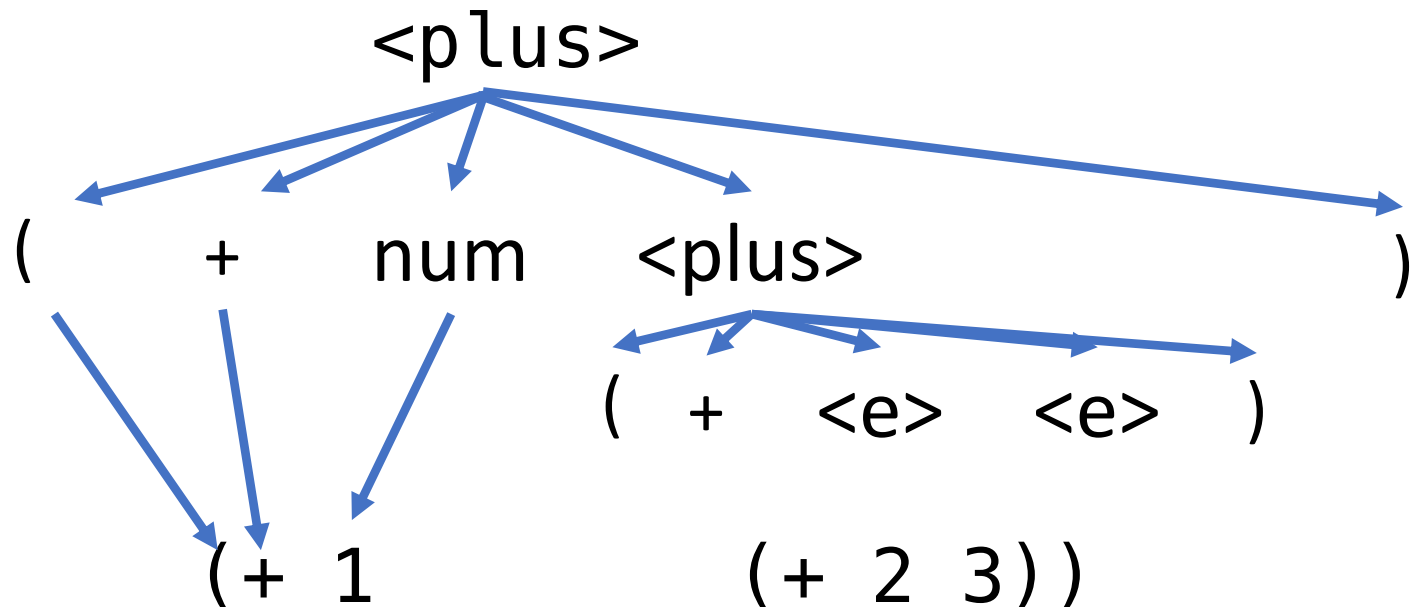
Parsing with BNF

`<plus> ::= (+ <e> <e>)`
`<e> ::= num | <plus>`
`<start> ::= <e>`



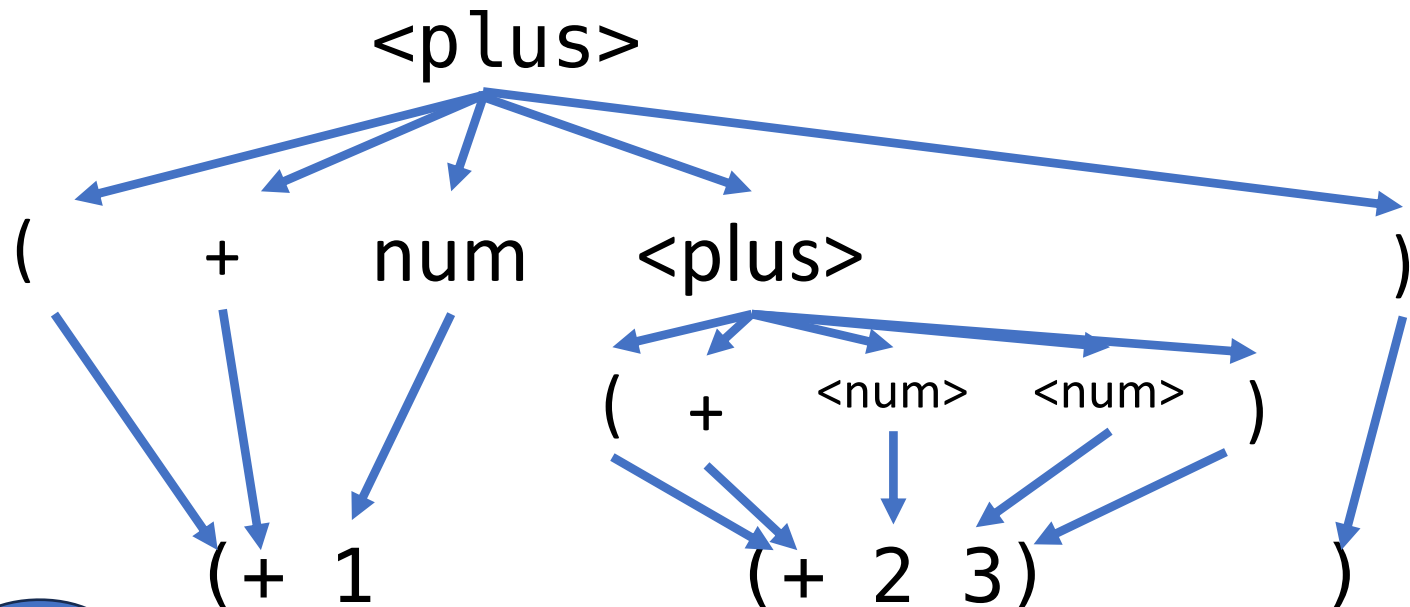
Parsing with BNF

$\langle \text{plus} \rangle ::= (+ \langle e \rangle \langle e \rangle)$
 $\langle e \rangle ::= \text{num} \mid \langle \text{plus} \rangle$
 $\langle \text{start} \rangle ::= \langle e \rangle$



Parsing with BNF

$\langle \text{plus} \rangle ::= (+ \langle e \rangle \langle e \rangle)$
 $\langle e \rangle ::= \text{num} \mid \langle \text{plus} \rangle$
 $\langle \text{start} \rangle ::= \langle e \rangle$



This diagram is called a *parse tree*

Parse errors

```
<plus> ::= (+ <e> <e>)  
<e>    ::= num | <plus>  
<start> ::= <e>
```

- A **parse error** occurs when there are no rules to apply

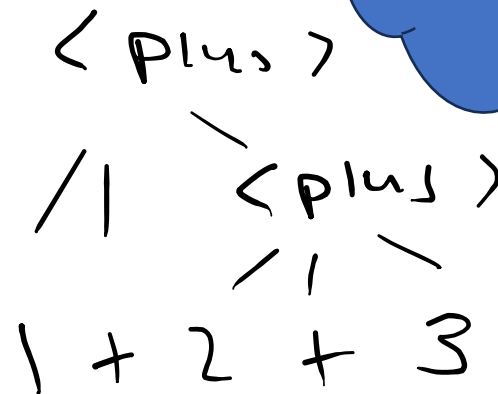
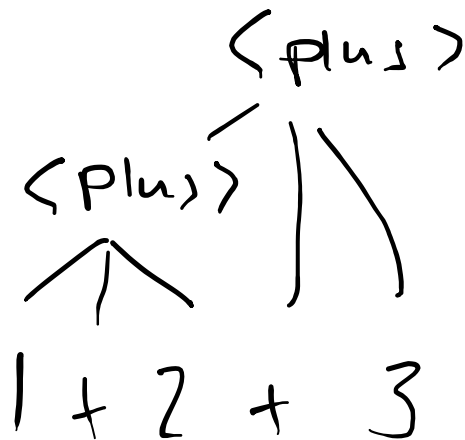
+ 1 2)

Parsing ambiguity

- Suppose we have the following grammar for infix addition:

$$\begin{aligned} \langle \text{plus} \rangle & ::= \langle e \rangle + \langle e \rangle \\ \langle e \rangle & ::= \text{num} \mid \langle e \rangle + \langle e \rangle \end{aligned}$$

- Then, we have two valid parse trees:



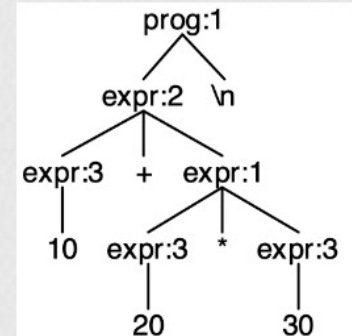
If there exists a sentence with more than 1 parse tree, we call a grammar ***ambiguous***

Parsing with BNF

- There are many tools that, given a BNF grammar, automatically generate a parser for you
- Example: antlr <https://www.antlr.org/>

```
grammar Expr;  
prog: (expr NEWLINE)* ;  
expr: expr ('*' | '/') expr  
      | expr ('+' | '-') expr  
      | INT  
      | '(' expr ')'  
      ;  
NEWLINE : [\r\n]+ ;  
INT      : [0-9]+ ;
```

```
$ antlr4-parse Expr.g4 prog -gui  
10+20*30  
^D  
$ antlr4 Expr.g4 # gen code  
$ ls ExprParser.java  
ExprParser.java
```



Parsing with s-expressions in Plait

- We don't need to worry about going from strings to plait datatypes: we can use Plait's parser

```
`(+ 1 2)  
- S-Exp  
`(+ 1 2)
```

Shorthand for:

```
(list->s-exp  
  (list (symbol->s-exp '+)  
        (number->s-exp 1)  
        (number->s-exp 2)))
```

From s-expressions to calc

```
(define-type Expr
  [num (n : Number)]
  [plus (l : Expr) (r : Expr)])

(parse : (S-Exp -> Expr))
(define (parse e)
  (cond
    [(s-exp-number? e) (num (s-exp->number e))]
    [else (error 'parse "unrecognized symbol")]))
```

From s-expressions to calc

```
(define-type Expr
  [num (n : Number)]
  [plus (l : Expr) (r : Expr)])

(parse : (S-Exp -> Expr))
(define (parse e)
  (cond
    [(s-exp-number? e) (num (s-exp->number e))]
    [(s-exp-list? e) ???]
    [else (error 'parse "unrecognized symbol")]))
```

An aside on `let` and `local`

- `local` defines a *new scope*: any definitions occurring inside `local` are only in scope from inside its body

```
> (local [(define x 10)] x)
- Number
10
```



List of definitions

```
> (local [(define x 10) (define y 30)] (+ x y))
- Number
40
```




Body

```
> (+ x y)
. x: free variable while typechecking in: x
```


An aside on `let` and `local`

- `let` declares local variables (short-hand for `local`):



List of variable
declarations


```
> (let [(x 10) (y 20)] (+ x y))  
- Number  
30
```



Body

letrec

- letrec declares local variables that can refer to each other:



List of variable declarations

```
> (letrec [(x 10) (y (+ x 20))] (+ x y))  
- Number  
40
```



Body

From s-expressions to calc

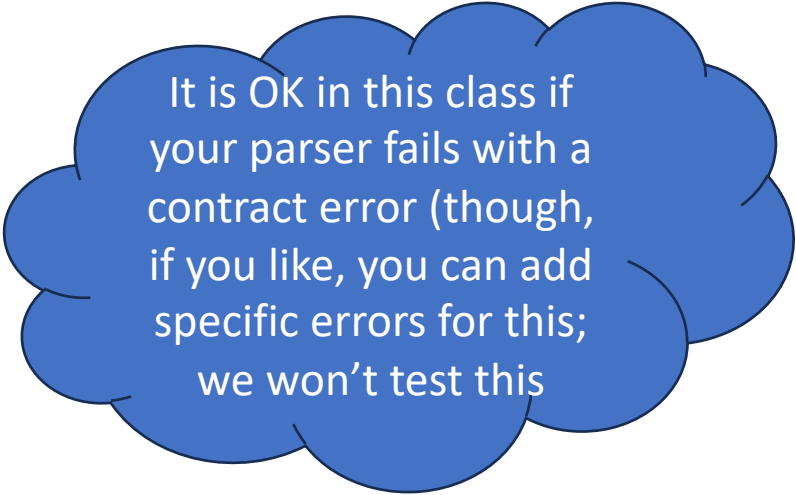
```
(define-type Expr
  [num (n : Number)]
  [plus (l : Expr) (r : Expr)])

(parse : (S-Exp -> Expr))
(define (parse e)
  (cond
    [(s-exp-number? e) (num (s-exp->number e))]
    [(s-exp-list? e)
     (let ([l (s-exp->list e)])
       (error 'parse ""))]
    [else (error 'parse "unrecognized symbol")]))
```

From s-expressions to calc

```
(define-type Expr
  [num (n : Number)]
  [plus (l : Expr) (r : Expr)])

(parse : (S-Exp -> Expr))
(parse : (S-Exp -> Expr))
(define (parse e)
  (cond
    [(s-exp-number? e) (num (s-exp->number e))]
    [(s-exp-list? e)
     (let ([l (s-exp->list e)])
       (cond
         [(empty? l) (error 'parse "empty list")]
         [(symbol=? (s-exp->symbol (first l)) '+) (plus (parse
(second l)) (parse (third l)))]
         [else (error 'parse "unrecognized symbol")])])])
    [else (error 'parse "unrecognized s-exp")])])
```



It is OK in this class if your parser fails with a contract error (though, if you like, you can add specific errors for this; we won't test this)

Conditionals

The language cond

<https://gist.github.com/SHoltzen/8ec4d0ec1619a623ff8a4779072eb660>

A proposed cond AST

```
(define-type Expr
  [num (n : Number)]
  [plus (l : Expr) (r : Expr)]
  [cnd (guard : Expr) (thn : Expr) (els : Expr)])
```

Semantics of `cond`

- Currently our calc language has a single value type: **numbers**
- One option for semantics of `COND`: if the guard is zero, evaluate the `then` branch; else evaluate the `else` branch

$(\text{cond } 10 \ 20 \ 30) \rightarrow 20$

Many languages have somewhat interesting semantics for **if**...

main.c	  Save Run	Output
<pre data-bbox="208 468 1132 1293">1 // Online C compiler to run C program online 2 #include <stdio.h> 3 4 int main() { 5 // Write C code here 6 if(10) { 7 printf("1"); 8 } 9 if(0) { 10 printf("2"); 11 } 12 if(-1) { 13 printf("3"); 14 } 15 16 return 0; 17 }</pre>		<pre data-bbox="1244 468 1572 551">/tmp/T9huXgalyf.o 13 </pre>

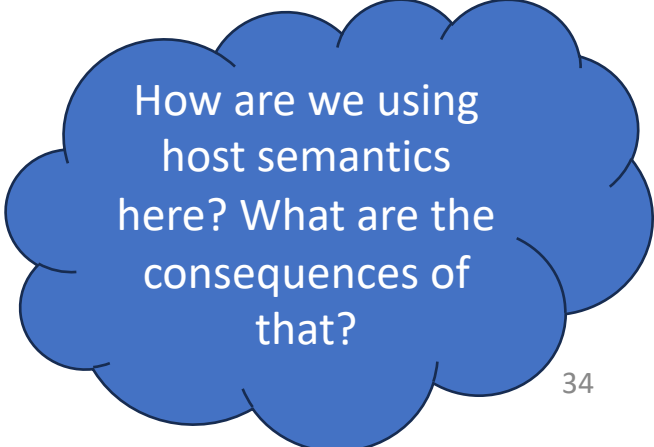
Many languages have somewhat interesting semantics for **if**...

main.js	Output
<pre>1 // Online Javascript Editor for free 2 // Write, Edit and Run your Javascript code using JS Online Compiler 3 4 if(0) { 5 console.log("0 is true"); 6 } 7 if(1) { 8 console.log("1 is true"); 9 } 10 if("wat") { 11 console.log("hmm"); 12 } 13 if("") { 14 console.log("!?"); 15 }</pre>	<pre>node /tmp/M76UL60pni.js 1 is true hmm</pre>

An evaluator

```
(define-type Expr
  [num (n : Number)]
  [plus (l : Expr) (r : Expr)]
  [cnd (guard : Expr) (thn : Expr) (els : Expr)])
```

```
(define (calc e)
  (type-case Expr e
    [(num v) v]
    [(plus l r) (+ (calc l) (calc r))]
    [(cnd guard thn els)
     (if (equal? 0 (calc guard))
         (calc thn)
         (calc els))]))
```



How are we using
host semantics
here? What are the
consequences of
that?

Cond with Booleans: Syntax

```
(define-type Exp
  [num (n : Number)]
  [bool (b : Boolean)]
  [plus (left : Exp) (right : Exp)]
  [cnd (test : Exp) (thn : Exp) (els : Exp)])
```

Cond with Booleans: Semantics

- If the guard evaluates to $\#t$, evaluate thn ; if guard evaluates to $\#f$, evaluate els ; otherwise, error

(if true 10 20) \rightarrow 10

Developing an evaluator

- We will walk through developing this in class:

<https://gist.github.com/SHoltzen/8ec4d0ec1619a623ff8a4779072eb660>